ECN 106 : Decision Making

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WINTER 2024 - SECOND MIDTERM EXAM: | ANSWERS for VERSION 1

- **1.** (a) The information is (1) P(D) = 0.02 (from which we deduce that $P(\neg D) = 0.98$), (2) P(-|D) = 0.01 (from which we deduce that P(+|D) = 0.99) and (3) P(+|-D) = 0.05. Now, P(+) = P(+|D)P(D) + P(+|D)P(D) = 0.99(0.02) + 0.05(0.98) = 0.0688 = 6.88%.
 - (b) 2% of 10,000 is 200; thus 200 have the disease and 9,800 don't. Of the 200 who have the disease, 1%, that is, 2 give a negative result; thus the remaining 198 give a positive result. Of the 9,800 who don't have the disease, 5% (that is, 490) give a positive result. Thus the table is as follows:

	positive blood test	negative blood test	Total
have the disease	198	2	200
don't have the disease	490	9,310	9,800
Total	688	9,312	1

(c)
$$\frac{490}{688} = 0.7122 = 71.22\%$$
.

- 2. (a) Putting the money in the checking account corresponds to the lottery $\binom{\$1,200}{1}$, whose expected value is 1,200, while putting it in the mutual fund corresponds to the lottery $\begin{pmatrix} \$1,800 & \$1,400 & \$700 \\ \frac{8}{100} & \frac{74}{100} & \frac{18}{100} \end{pmatrix}$ whose expected value is 1,306. Hence Trevor would be risk averse.
 - (b) The possible levels of wealth are: \$1,800, \$1,400, \$1,200 and \$700. Assign utility 1 to \$1,800 and zero to \$700. Since $\underbrace{\begin{pmatrix} \$1,400 \\ 1 \end{pmatrix}}_{CD} \sim \underbrace{\begin{pmatrix} \$1,800 & \$700 \\ \frac{1}{2} & \frac{1}{2} \end{pmatrix}}_{startup}$

$$\frac{1}{2}1 + \frac{1}{2}0 = \frac{1}{2} = 0.5 \text{. Finally, since } \underbrace{\begin{pmatrix} \$1,200 \\ 1 \end{pmatrix}}_{Checking} \sim \underbrace{\begin{pmatrix} \$1,400 & \$700 \\ \frac{96}{100} & \frac{4}{100} \end{pmatrix}}_{foreign venture}, \text{ the utility of $1,200 is }$$

$$\frac{96}{100}$$
0.5 + $\frac{4}{100}$ 0 = 0.48. Hence Trevor's utility function is $\begin{cases} $1,800 $ 1,400 $ 1,200 $ 700 \\ 1 0.5 0.48 & 0 \end{cases}$

- (c) $\mathbb{E}[U(checking)] = 0.48$, $\mathbb{E}[U(mutual)] = \frac{8}{100}1 + \frac{74}{100}0.5 + \frac{18}{100}0 = 0.45$ $\mathbb{E}[U(CD)] = 0.5$, $\mathbb{E}[U(startup)] = 0.5(1) + 0.5(0) = 0.5$, $\mathbb{E}[U(foreign)] = \frac{96}{100} \cdot 0.5 + \frac{4}{100} \cdot 0 = 0.48$.
- (d) For a risk neutral person we compute expected values. $\mathbb{E}[checking] = 1,200$, $\mathbb{E}[mutual] = \frac{8}{100}1,800 + \frac{74}{100}1,400 + \frac{18}{100}700 = 1,306$, $\mathbb{E}[CD] = 1,400$, $\mathbb{E}[startup] = 0.5(1,800) + 0.5(700) = 1,250$, $\mathbb{E}[foreign] = \frac{96}{100}1,400 + \frac{4}{100}700 = 1,372$. Thus the ranking is $CD \succ foreign \succ mutual \succ startup \succ checking$.

3.

regret table is: $\begin{vmatrix} -\frac{1}{3} & \frac{s_1}{7} & \frac{s_2}{7} & \frac{s_3}{6} & \frac{s_4}{0} \\ b & 6 & 0 & 7 & 1 \\ c & 0 & 12 & 0 & 9 \end{vmatrix}$ where the maximum regret for each act is

highlighted.

- **(b)** The MinMax Regret solution is: $\{a,b\}$.
- (c) (c.1) $H(a, \frac{1}{4}) = 4 \times \frac{1}{4} + 9 \times \frac{3}{4} = \frac{31}{4} = 7.75$. (c.2) $H(b, \frac{1}{4}) = 3 \times \frac{1}{4} + 13 \times \frac{3}{4} = \frac{42}{4} = 10.5$. (c.1) $H(c, \frac{1}{4}) = 0 \times \frac{1}{4} + 11 \times \frac{3}{4} = \frac{33}{4} = 8.25$.
- (d) $\mathbb{E}[U(a)] = \frac{4+6+4+9}{4} = \frac{23}{4}$, $\mathbb{E}[U(b)] = \frac{5+13+3+8}{4} = \frac{29}{4}$, $\mathbb{E}[U(c)] = \frac{11+1+10+0}{4} = \frac{22}{4}$ Thus the act that maximizes expected utility is b.