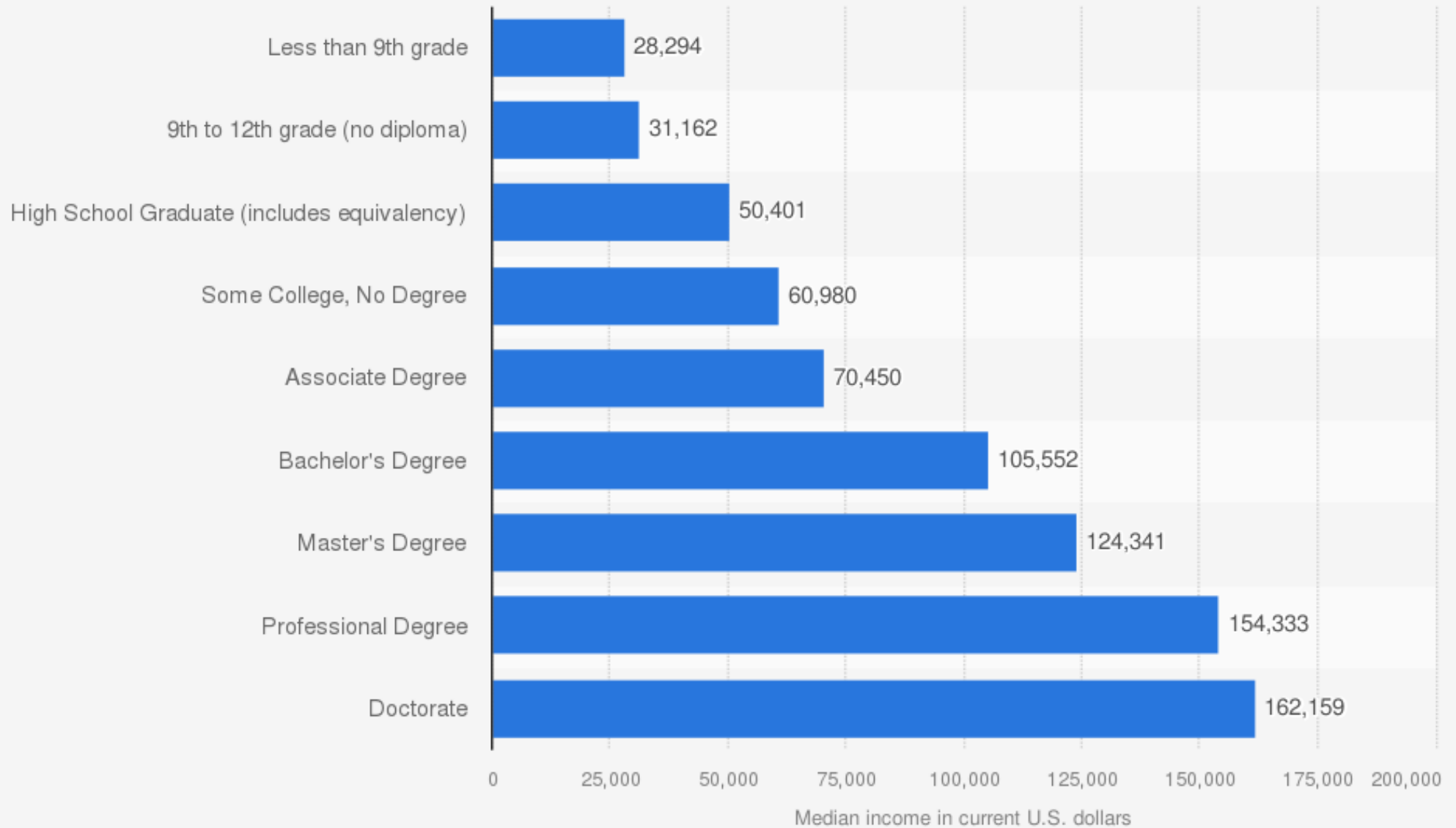


U.S. median household income 2021, by education level

Less than 9th grade	\$28,294
9th to 12th grade (no diploma)	\$31,162
High School Graduate	\$50,401
Some College, No Degree	\$60,980
Associate Degree	\$70,450
Bachelor's Degree	\$105,552
Master's Degree	\$124,341
Professional Degree	\$154,333
Doctorate	\$162,159

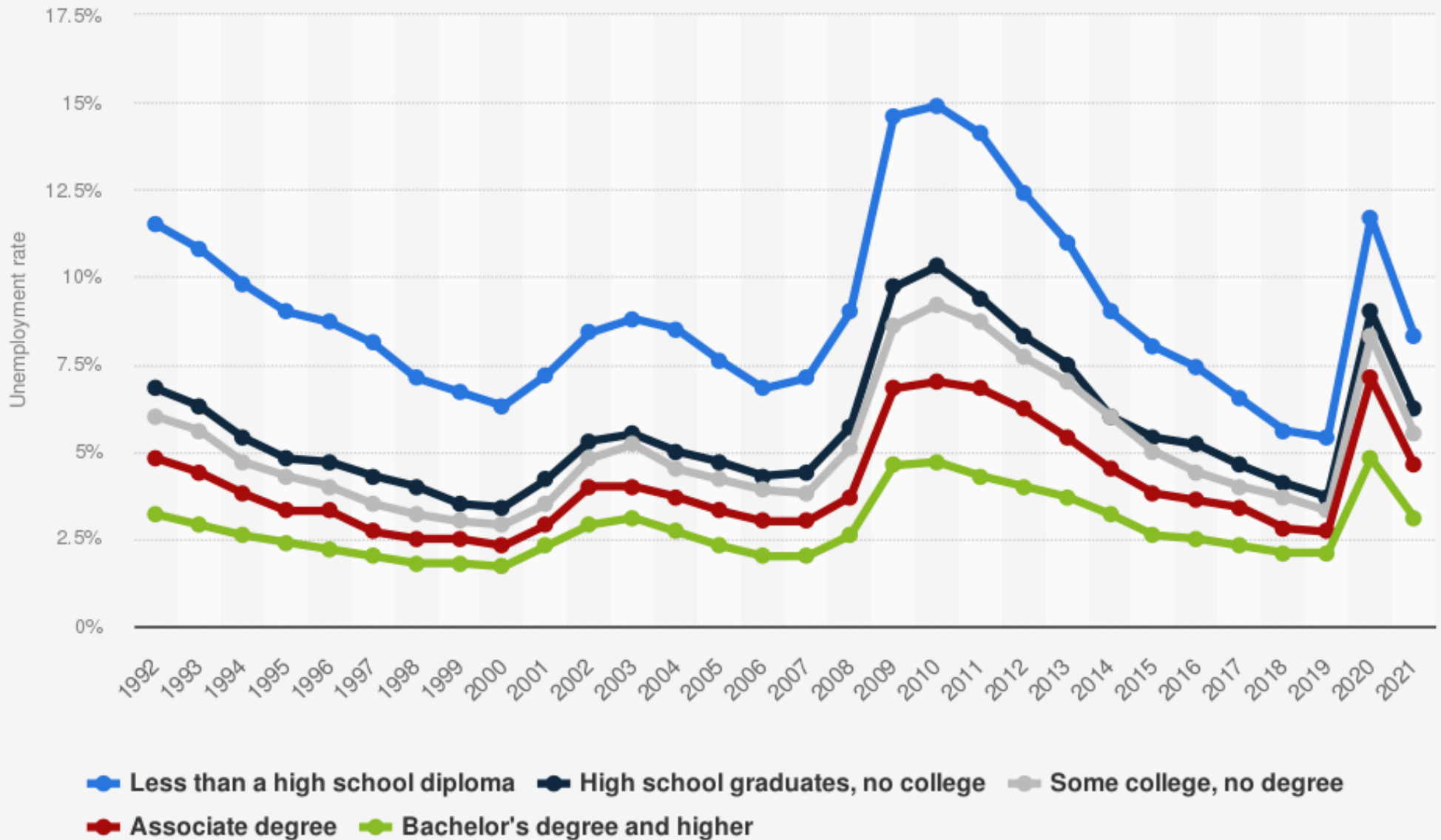
Median household income in the United States in 2021, by educational attainment of householder (in U.S. dollars)



Source
US Census Bureau
© Statista 2022

Additional Information:
United States; US Census Bureau; 2021

Unemployment rate in the United States from 1992-2021, by level of education



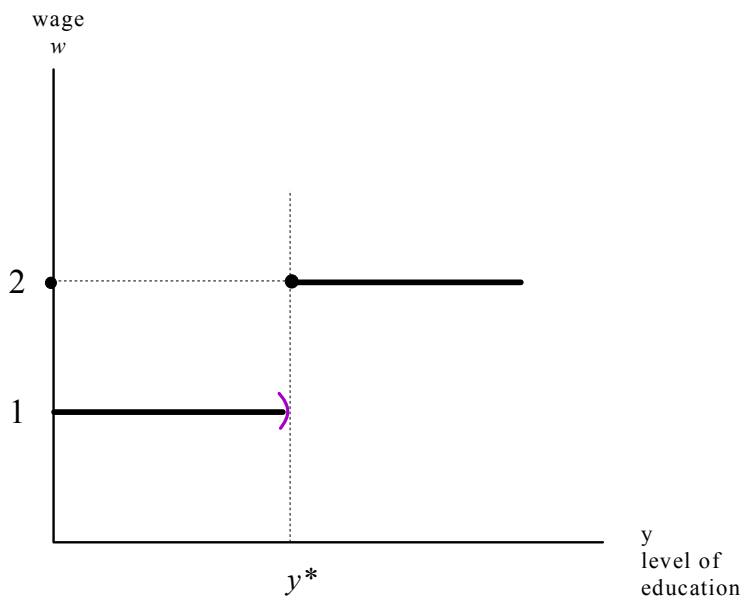
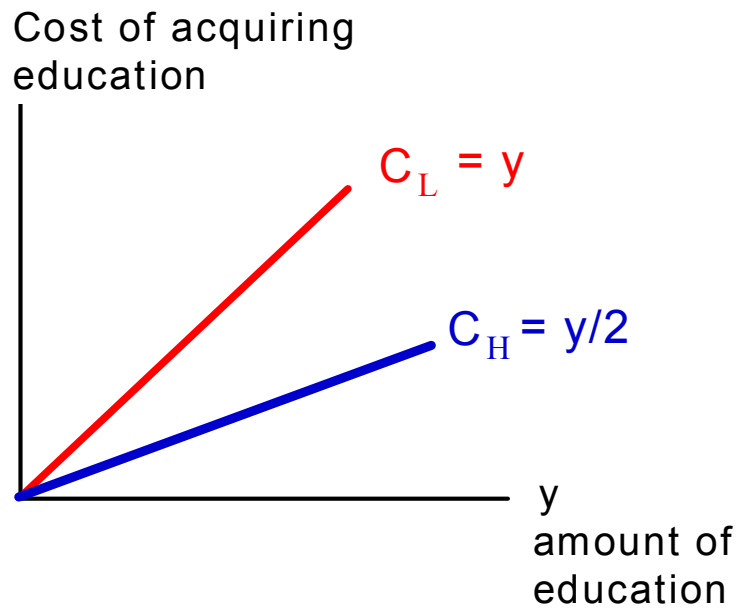
Source
Bureau of Labor Statistics
© Statista 2022

Additional Information:
United States; 1992 to 2021; 25 years and older

Suppose that there are two groups of individuals:

Group L	Group H
Marginal productivity = 1	Marginal productivity = 2
Proportion in population: q_L	Proportion in population: $1 - q_L$

with $0 < q_L < 1$.



Employers' wrong beliefs

$$C_L(y) = y$$

For a GROUP L individual

If choose $y = 0$

get $w = 1$

pay $C = 0$

net wage = $1 - 0 = 1$

If choose $y = y^*$

get $w = 2$

pay $C = y^*$

net wage = $2 - y^*$

$$C_H(y) = \frac{y}{2}$$

For a GROUP H individual

If choose $y = 0$

get $w = 1$

pay $C = 0$

net wage = $1 - 0 = 1$

If choose $y = y^*$

get $w = 2$

pay $C = \frac{y^*}{2}$

net wage = $2 - \frac{y^*}{2}$

Want L types to choose $y = 0$: $1 > 2 - y^*$

$$y^* > 1$$

Want H types to choose $y = y^*$: $2 - \frac{y^*}{2} > 1$

if $1 < y^* < 2$ then L choose $y = 0$ paid 1 (= true prod.)
 H " " $y = y^*$ " 2 (=)

$$y^* < 2$$

Before (assuming $1 < y^* < 2$) $\left\{ \begin{array}{l} L \quad y=0 \quad \text{net wage} = 1 \\ H \quad y=y^* \quad \text{net wage} = 2 - \frac{y^*}{2} \end{array} \right.$

Can a signaling equilibrium be Pareto inefficient?

On average employers were paying

$$q_L \cdot 1 + (1 - q_L) \cdot 2 \quad \text{per employee}$$

Government closes down all schools, instructs employers

L people "choose" $y=0$. to pay $q_L + (1 - q_L) \cdot 2$
to everybody

net wage: $q_L + (1 - q_L) \cdot 2 = 2 - q_L > 1$ since $q_L < 1$

L people are better off

H people "choose" $y=0$, net wage is

$$2 - q_L$$

They are better off if $2 - q_L > 2 - \frac{y^*}{2}$

$$\frac{y^*}{2} > q_L$$

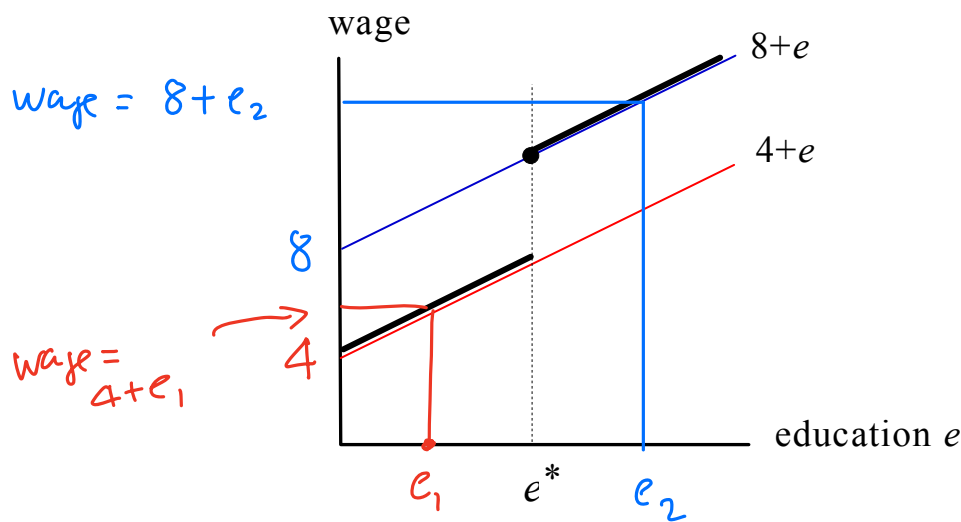
Example: $y^* = 1.5$

$$q_L = 0.5$$

$$\frac{y^*}{2} = \frac{1.5}{2} = 0.75$$

Example of a signaling equilibrium when education does increase productivity

Type L: $\begin{cases} \text{productivity: } 4+e \\ \text{cost: } C_L(e) = 4e \end{cases}$ and **Type H:** $\begin{cases} \text{productivity: } 8+e \\ \text{cost: } C_H(e) = 2e \end{cases}$



For a signaling equilibrium we need:

for Type L: $\begin{cases} \text{if } e < e^* \text{ then } e=0 \text{ net} = 4-0 = 4 \\ \text{if } e \geq e^* \text{ then } e=e^* \text{ net} = 8+e^* - 4e^* \end{cases}$

for Type H: $\begin{cases} e=0 & \text{net} = 4 \\ e=e^* & \text{net} = 8+e^* - 2e^* \end{cases}$